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The recent similarity hypotheses to describe water infiltration into homogeneous soils

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ABSTRACT: A similarity hypothesis recently presented to describe horizontal infiltration into homogeneous soils, developed for coarse-textured soils like sieved marine sand, implies that the soil water retention function $\theta(h)$ is the mirror image of an extended Boltzmann transform function $\theta(\lambda^2)$. A second hypothesis applicable to vertical infiltration suggests that the soil water retention function $\theta(h)$ is also the mirror image of the soil water profile $\theta(z)$. Using previously published infiltration data, we investigated whether these two similarity solutions successfully describe infiltration into two “normal” soils. Although the theory using the first similarity assumption adequately describes horizontal cumulative infiltration and infiltration rate into both soils, it fails to estimate soil water distributions measured between soil profiles. The second similarity solution for vertical infiltration into either soil completely fails to coincide with measured soil water distributions, cumulative infiltration and infiltration rate.

Keywords: Boltzmann function, mirror image, wetting front

Introduction

Hydraulic transport and retention properties of water-unsaturated soils are strikingly complex, therefore, obtaining simple solutions for describing infiltration into soils remains a lingering challenge. After the classical concepts of Darcy (1856), Boltzmann (1894) and Buckingham (1907), Green and Ampt (1911) developed an equation to estimate water infiltration into a sandy soil subjected to specific initial and boundary conditions. Today, the Green and Ampt equation as well as Richard's equation (1931), developed while he conducted research for his PhD degree, are now commonplaces in soil physics and hydrology textbooks. Moreover, since Philip (1955) published a numerical solution of Richard's equation for water infiltrating into a homogeneous soil, his achievement has been universally used as a classical solution known as the Richard's equation.

Recently, Prevedello et al. (2008) focused on soil water content distribution $[\theta(x,t)]$ during horizontal infiltration to estimate infiltration into homogeneous soils using measured values of K for specific values of θ and the soil water retention curve $\theta(h)$, Richard's equation and an extension of the historic 1894 Boltzmann transform function. As illustrated in Figure 1A, this similarity hypothesis

$$h \frac{d\theta}{dh} = \lambda^2 \frac{d\theta}{d\lambda^2} \quad (1)$$

implies that the soil water retention function $\theta(h)$ is the mirror image of an extended Boltzmann transform function $\theta(\lambda^2)$. For vertical infiltration, Prevedello et al. (2009) published another similarity hypothesis

$$h \frac{d\theta}{dh} = z \frac{d\theta}{dz} \quad (2)$$

illustrated in Figure 1B and showed that $\theta(h)$ is the mirror image of the soil water profile $\theta(z)$.

Recognizing that these similarity solutions are approximations of classical solutions of Richard's equation,

Prevedello et al. (2008, 2009) specifically stated that the use and acceptance of the hypotheses remained open for future research. Here, without deriving additional mirror image hypotheses, we merely explore the potential use and associated restrictions of the two recent similarity hypotheses illustrated in Figure 1.

Theory

Similarity solution for horizontal infiltration

With the analytic integral of Eq. [1] introduced into the equation of continuity subject to the initial and boundary conditions

$$\begin{aligned} \theta &= \theta_i & x &\geq 0 & t &= 0 \\ \theta &= \theta_0 & h &= h_0 & x &= 0 & t > 0 \\ \theta &= \theta_i & h &= h_i & x &\rightarrow \infty & t \geq 0 \end{aligned}$$

where subscript i refers to initial, 0 to saturated and t is the infiltration time.

Prevedello's similarity solution for horizontal infiltration is

$$x[h(\theta), t] = t^{1/2} \sqrt{-2h \int_{K_i}^{K_0} h dK / \int_{\theta(h_i)}^{\theta(h_0)} h d\theta} \quad (3)$$

Integrating Eq. [3] between the boundary conditions θ_i and θ_0 , the cumulative infiltration $i(t)$ at the soil surface $x = 0$ is

$$i(t) = t^{1/2} \int_{\theta_i}^{\theta_0} |h|^{1/2} d\theta \sqrt{2 \int_{h_i}^{h_0} K dh / \int_{\theta(h_i)}^{\theta(h_0)} h d\theta} \quad (4)$$

The derivative of Eq. [4] with respect to time t defines the infiltration rate $q_0(t)$ at the soil surface

$$q_0(t) = \frac{1}{2t^{1/2}} \int_{\theta_i}^{\theta_0} |h|^{1/2} d\theta \sqrt{2 \int_{h_i}^{h_0} K dh / \int_{\theta(h_i)}^{\theta(h_0)} h d\theta} \quad (5)$$

Similarity solution for vertical downward infiltration

After introducing Eq. [2] into Richards' equation and integrating it subject to the initial and boundary conditions

$$\begin{aligned} \theta &= \theta_i & z &\geq 0 & t &= 0 \\ \theta &= \theta_0 & h &= h_0 & z &= 0 & t > 0 \\ \theta &= \theta_i & h &= h_i & z &\rightarrow \infty & t \geq 0 \end{aligned}$$

where subscript *i* refers to initial, 0 to saturated and *t* is the infiltration time.

Prevedello's similarity solution for vertical downward infiltration is

$$\frac{(K_0 - K_i)t}{(\theta_0 - \theta_i)} = z + (h - h_0) \ln \left(1 - \frac{z}{h - h_0} \right) \quad (6)$$

The soil water content profile $\theta(z, t)$ during infiltration is obtained from Eq. [6] using measured values of the soil water retention curve.

Materials and Methods

The similarity solutions of Prevedello et al. (2008 and 2009) are here tested with measurements of water infiltrating into laboratory columns of Columbia silt loam and Hesperia sandy loam (Davidson et al., 1963). Their measured soil water properties and wetting parameters are given in Table 1.

During horizontal and vertical infiltration into the Columbia and Hesperia soils, the matric potential head

h_0 at their soil surfaces was maintained at -2 cm. Values of $x[h(\theta), t]$, $i(t)$ and $q_0(t)$ from Eqs. [3 through 5] as well as $\theta(z, t)$ obtained from Eq. [6] were compared with those from classical solutions of the Richards' equation derived by Philip (1955).

Results and Discussion

Horizontal infiltration

Calculations made from Eqs. [3, 4 and 5] presented in Figures 2 through 4 illustrate the comparisons of the Prevedello similarity solutions to measured observations and classical solutions of Richards' equation for three different infiltration times. From Figure 2, it is readily apparent that all of the similarity calculations for the Marine sand are nearly identical to those stemming from the classical solution of Philip, as stated in Prevedello et al. (2008).

Based on the Columbia silt loam measurements, graphs of soil water content profiles, cumulative infiltration and infiltration rate are presented in Figure 3. Indeed, cumulative infiltration and infiltration rate derived from the similarity solution successfully approximate those from the classical solution. However, it is immediately obvious that the similarity solution fails to estimate the distributions of the soil water measured within the profile. The similarity solution describes gradually flattening sigmoid-shaped wetting fronts rather than the persistently abrupt measured wetting fronts and those calculated from the classical solution of Richards' equation.

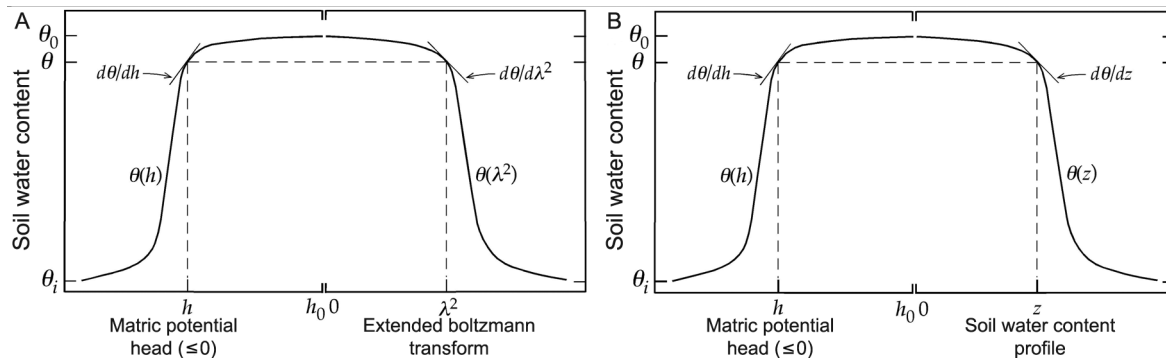


Figure 1 – A: Illustration of similarity hypothesis between $\theta(h)$ and $\theta(\lambda^2)$ for horizontal infiltration, and B: Illustration of similarity hypothesis between $\theta(h)$ and $\theta(z)$ for vertical downward infiltration.

Table 1 – Saturated hydraulic conductivity K_0 , saturated volumetric water content θ_0 , residual water content θ_r , initial water content θ_i , and wetting parameters of van Genuchten (1980) α , ℓ , m and n for Marine sand, Columbia silt loam and Hesperia sandy loam, used to calculate $\theta(h)$ and $K(\theta)$ functions by Mualem (1976).

Soil	K_0	θ_0	θ_i	θ_r	α	ℓ	m	n
	cm min ⁻¹		cm ³ cm ⁻³		cm ⁻¹			
Marine ¹	0.9498	0.387	0.037	0.037	0.0410	0.50	0.9412	17.00
Columbia ²	0.0464	0.450	0.031	0.020	0.01185	0.50	0.5078	2.032
Hesperia	0.1140	0.385	0.026	0	0.03250	1.77	0.3506	1.540

¹Prevedello et al. (2008); ²Davidson et al. (1963).

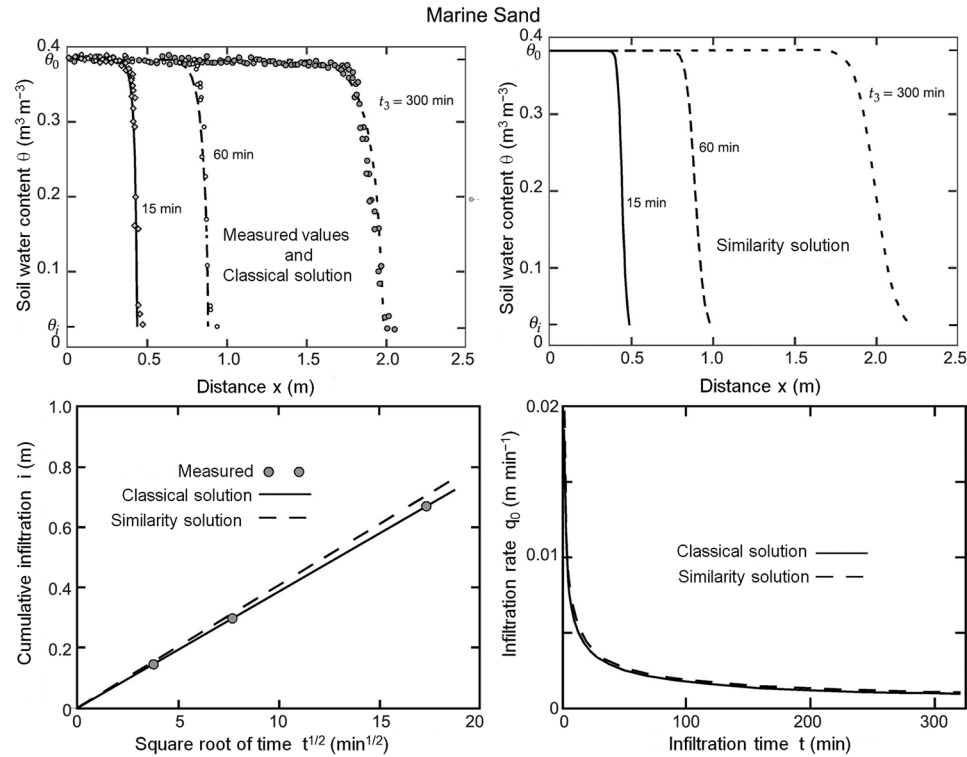


Figure 2 – Soil water content measured within horizontal columns of Marine sand as well as cumulative infiltration versus the square root of time and infiltration rate at soil surface as a function of time.

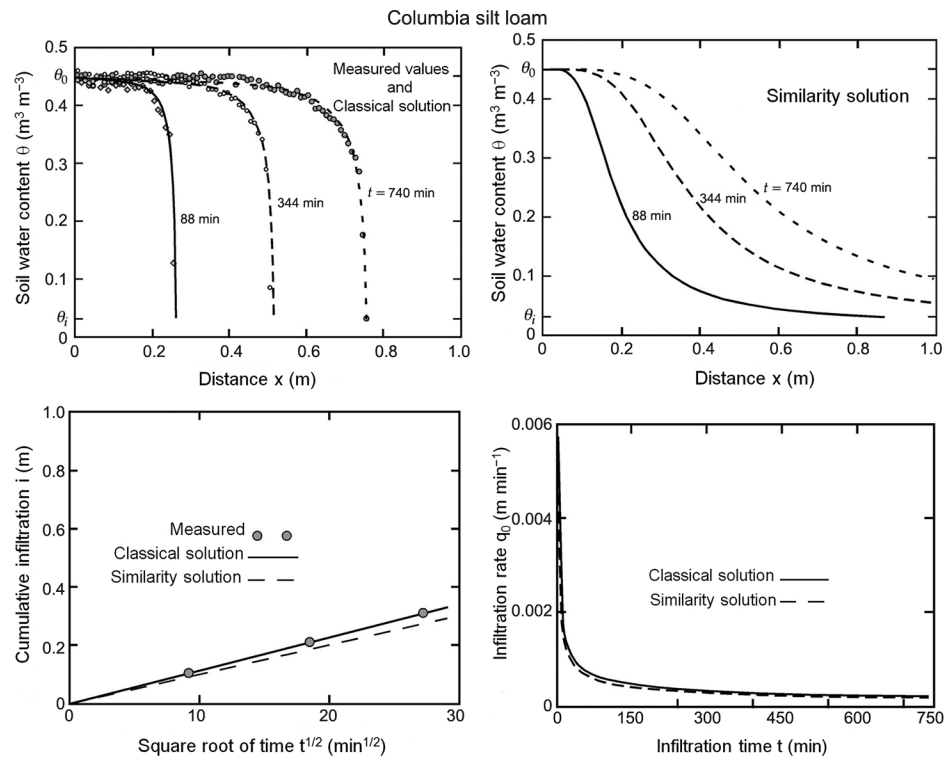


Figure 3 – Soil water content measured within horizontal columns of Columbia silt loam as well as cumulative infiltration versus the square root of time and infiltration rate at the soil surface as a function of time.

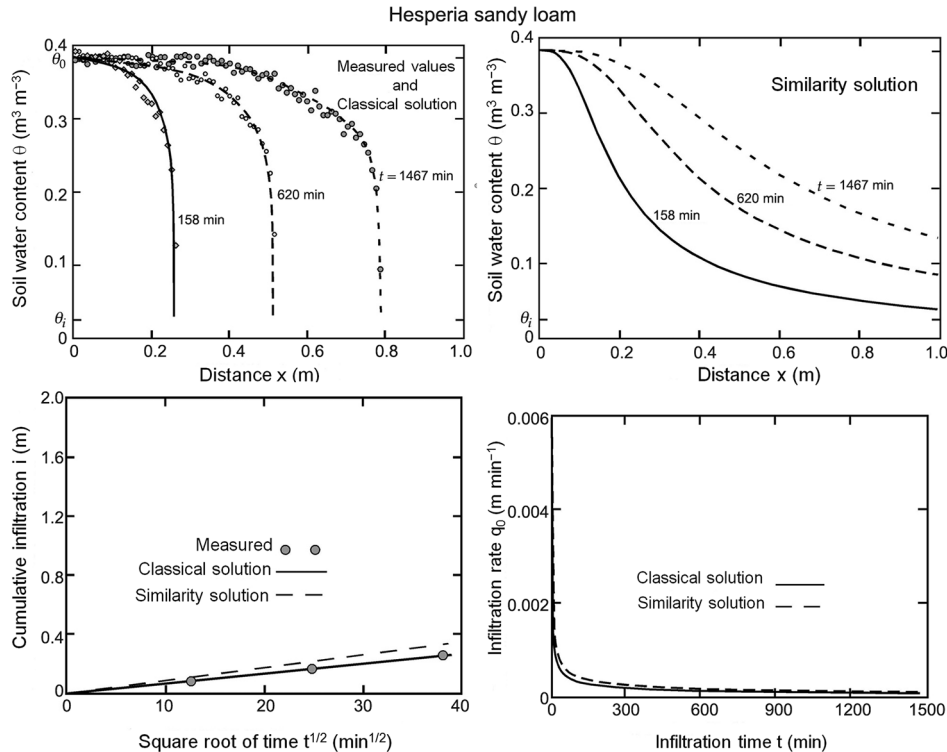


Figure 4 – Soil water content measured within horizontal columns of Hesperia sandy loam as well as cumulative infiltration versus the square root of time and infiltration rate at the soil surface as a function of time.

The results from the Hesperia sandy loam illustrated in Figure 4 are consistent with those from the Columbia silt loam. In other words, the similarity hypothesis successfully describes both cumulative infiltration and rate of infiltration, but fails to predict the abrupt shape of the measured wetting fronts.

Vertical infiltration

We now verify that Prevedello et al. (2009) was correct to limit the use of Eq. [6] to describe infiltration into only coarse textured soils. Figure 5 illustrates the results of using Eq. [6] to describe infiltration experiments into vertical columns of the two fine-textured soils.

From the figure, we first verify and notice for both soils that the measured soil water content distributions are accurately described by the classical solution of Richards' equation using measured soil water properties and wetting parameters given in Table 1. Hence, we are confident that the soil water content distributions calculated with the similarity solution Eq. [6] based on those same properties and parameters are erroneous and do not come close to reality. Indeed, the cumulative amounts of water infiltrating the Columbia profile calculated from the similarity solution are more than 2 times greater than reality. And the results observed for the Hesperia soil are also erroneous – the similarity calculations are more than 5 times greater than experimentally measured values. From these re-

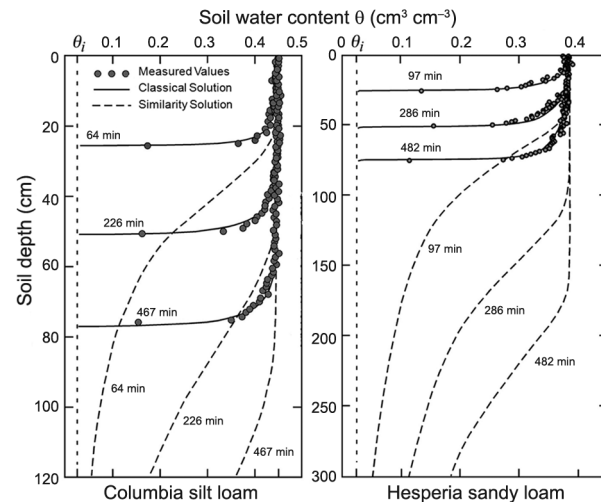


Figure 5 – Measured, classical solutions and similarity solutions of soil water content within vertical columns of Columbia silt loam and Hesperia sandy loam during vertical infiltration.

sults, we conclude that the utility of the 2009 Prevedello similarity assumption is correctly limited to coarse-textured soils.

Looking Ahead

We anticipate further attempts to create mirror images of soil water profiles, soil water functions and

related properties during infiltration and redistribution. Achieving simple solutions for water transport and retention in soils of different physical and chemical characteristics during this century shall remain a lingering challenge for soil scientists.

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